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**Stimulated Raman effect**

Stimulated Raman scattering (SRS) is an effective method to detect the oscillation of molecules and Raman spectroscopy is commonly used to provide a 'fingerprint' to identify the molecules. [1] In a solid, the interaction between light and lattice vibrations (phonons) takes place via absorption or emission of a photon, leading to an Anti-Stokes or Stokes shift of the photon as shown in figure (1).

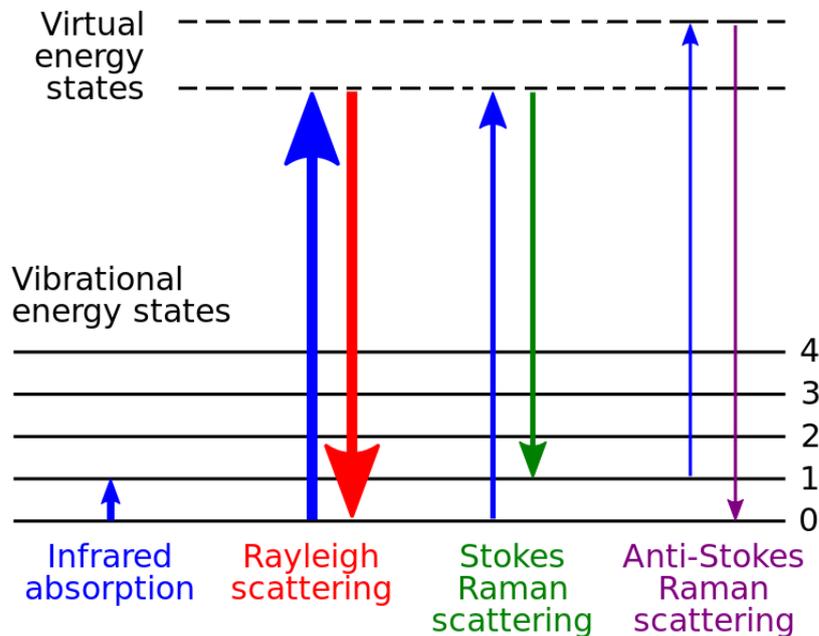


Figure 1: Graphic explanation of SRS. [1]

The frequency of the stokes line  $\omega_s = \omega - \Omega$ , and the anti-stokes line  $\omega_{as} = \omega + \Omega$ , where  $\Omega$  is the oscillation frequency of the phonons.

1. Assuming pump  $\omega$  and signal  $\omega_s$  ( $\omega_s$  is the frequency of the stokes line) pass through a Raman active medium as shown in figure (2). If we only consider the

third order nonlinear effect ( $\chi^{(3)}$ ), write down the coupled wave equation of the pump  $\omega$  and the signal  $\omega_s$ .

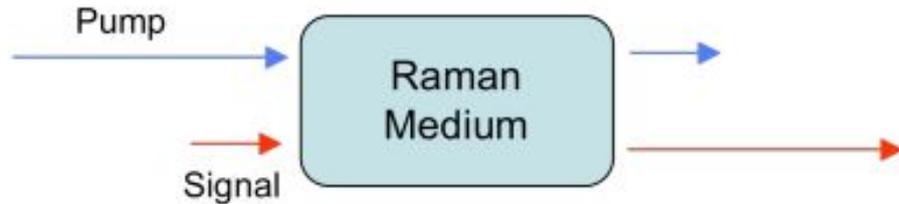


Figure 2: Graphic explanation of SRS. [2]

NOTE: for the signal, there are two effects. One is related to the stimulated Raman effect  $\chi_R^{(3)}$ , the other is related to 4-wave-mixing  $\chi_F^{(3)}$ .

2. Show that the stimulated raman effect doesn't need to be phase matched but the 4-wave-mixing needs to be phase matched.
3. By assuming that on the non-phase-matched condition (the 4-wave-mixing effect is small, so that could be neglected) and the pump is undepleted ( field of the pump is constant), solve the wave equation of the signal.

## References

- [1] Wikipedia, "Raman spectroscopy — wikipedia, the free encyclopedia." [https://en.wikipedia.org/w/index.php?title=Raman\\_spectroscopy&oldid=747734915](https://en.wikipedia.org/w/index.php?title=Raman_spectroscopy&oldid=747734915), 2016. [Online; accessed 18-November-2016].
- [2] C. T. A. Brown, "Lecture 6:  $\chi^3$  -based raman phenomena." <http://www.st-andrews.ac.uk/~ctab/PH4027/NLO-Lecture6-Notes.pdf>. [Online; accessed 18-November-2016, University of St Andrews].